


# **Fairness of Selection: Paradoxes and Dilemmas**

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A PLACE 4 OUT OF 5 AMERICAN HIGH  
SCHOOL STUDENTS HOPE TO VISIT

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# Outline

- Analysis of fairness ◻
- Any solutions? ◻



# How to Analyze Fairness?

- Alternative approaches to the analysis of fairness of selection
  - analysis of probability of admission ◻
  - regression analysis ◻
- First dilemma: should criterion be based purely on the event of admission or predicted success during the study?

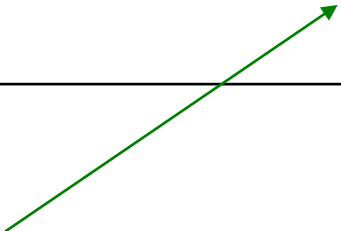
# Berkeley Study

- Bickel, P.J, Hammel, E.A., O'Connell, J.W., (1975). Sex bias in graduate admission: Data from Berkeley. *Science*, 7, 398-404.
- Data
  - 12,763 applicants (8,442 males; 4,321 females)
  - 101 different PhD programs
- 2x2-table with counts of admissions showed substantial sex bias ( $\chi^2=110.8$ ,  $df=1$ ,  $p=0$ )

# Berkeley Study *Cont'd*

	Admitted	Rejected
Males	3.738 (3.460,7)	4.704 (4.981,3)
Females	1.494 (1.771,3)	2.827 (2.549,7)

Observed-Expected  
 equal to -277.3



# Berkeley Study *Cont'd*

- Repetition of same analysis for 101 separate PhD programs showed 10 programs with significant differences
  - 4 programs discriminated against females (26 fewer females admitted than expected)
  - 6 programs discriminated against males (64 more females admitted than expected)
- What has happened to the  $277,3 + 26 - 64 = 239.3$  missing females?

# High School Exit Exam Study

- Study of developments in scores for German and French as a foreign language on Dutch high school exit exam between 1985-1990 (de Jong)
  - All scores equated (adjusted for differences in difficulty, etc.)
  - Scores in each track (Mavo/Havo/VWO) decreased systematically

# High School Exit Exam Study

*Cont'd*

- Study of developments in scores
  - Score distribution for whole population remained constant
- What has happened to the students with the decreasing scores?

# Basketball Study

- Belief in *streak shooting*: *hits* have a higher probability of being followed by another *hit* than by a *miss*
- Several explanations, including the idea of a “hot hand”

# Basketball Study *Cont'd*

- Kahneman-Tversky study of the perception of runs: tendency to perceive longer runs no longer as random
- Controlled experiments
  - Runs in coin tosses
  - Basketball throwing (Gilovich & Tversky)

# Basketball Study *Cont'd*

- Wardrop, R. L. (1995). Simpson's paradox and the hot hand in basketball. *The American Statistician*, 49, 24-28.
  - Re-analysis of the Gilovich-Tversky data
  - Data for the individual players do not show any streak shooting
  - Combined data for all players do show streak shooting

# Medical Studies

- Success rates for kidney-stone procedures
  - All open procedures (A)
  - Percutaneous nephrolithotomy (B)

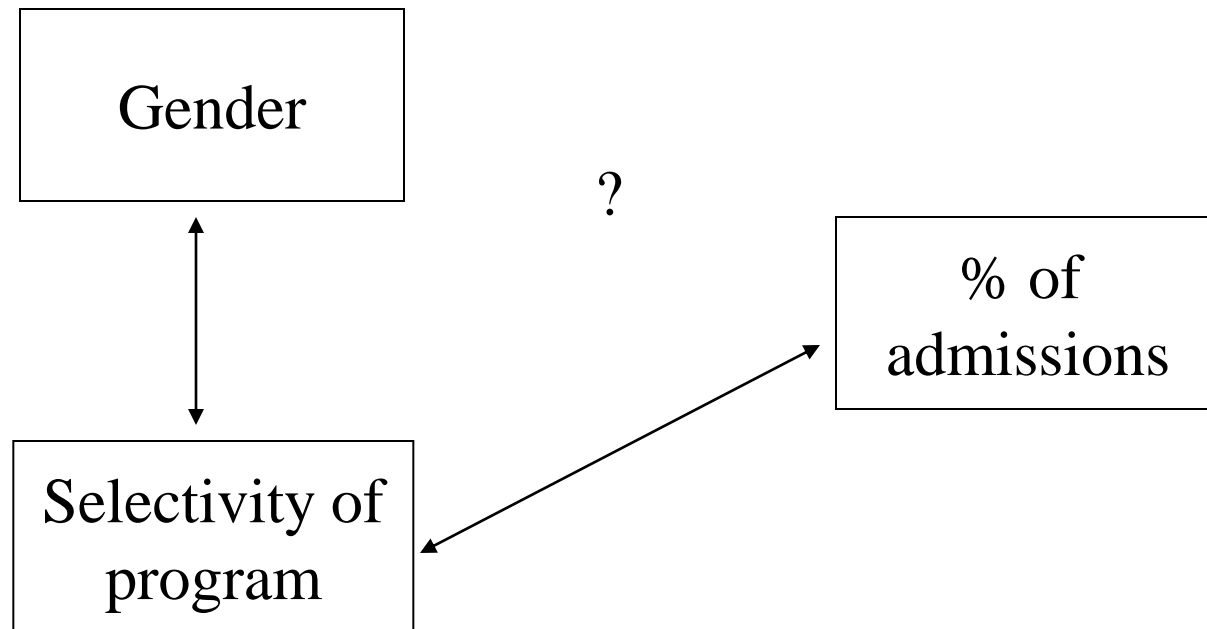
	A	B
Small Stones	<b>93%</b>	87%
Large Stones	<b>73%</b>	69%
Combined	78%	<b>83%</b>

# Simpson's Paradox

- The previous phenomena arise when covariates are present that correlate both with the independent and dependent variables
- Unawareness of such covariates leads to misleading results; acknowledgment leads to “paradoxes”
- Simpson's paradox occurs in correlational studies it is not a causal paradox

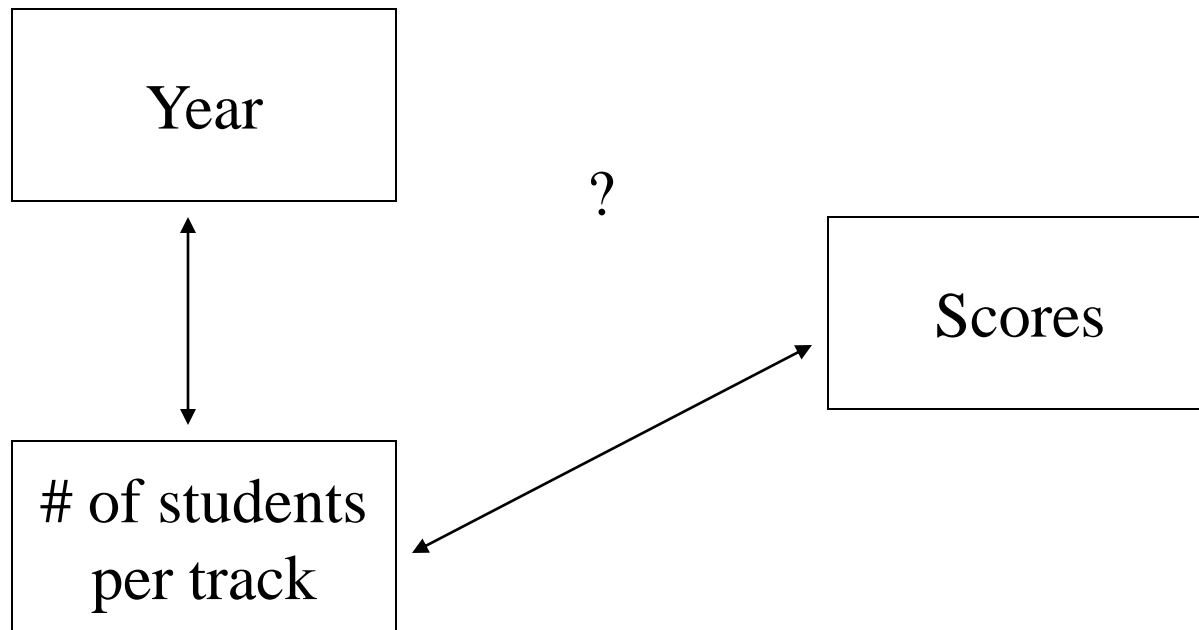
# Simpson's Paradox *Cont'd*

- Berkeley study



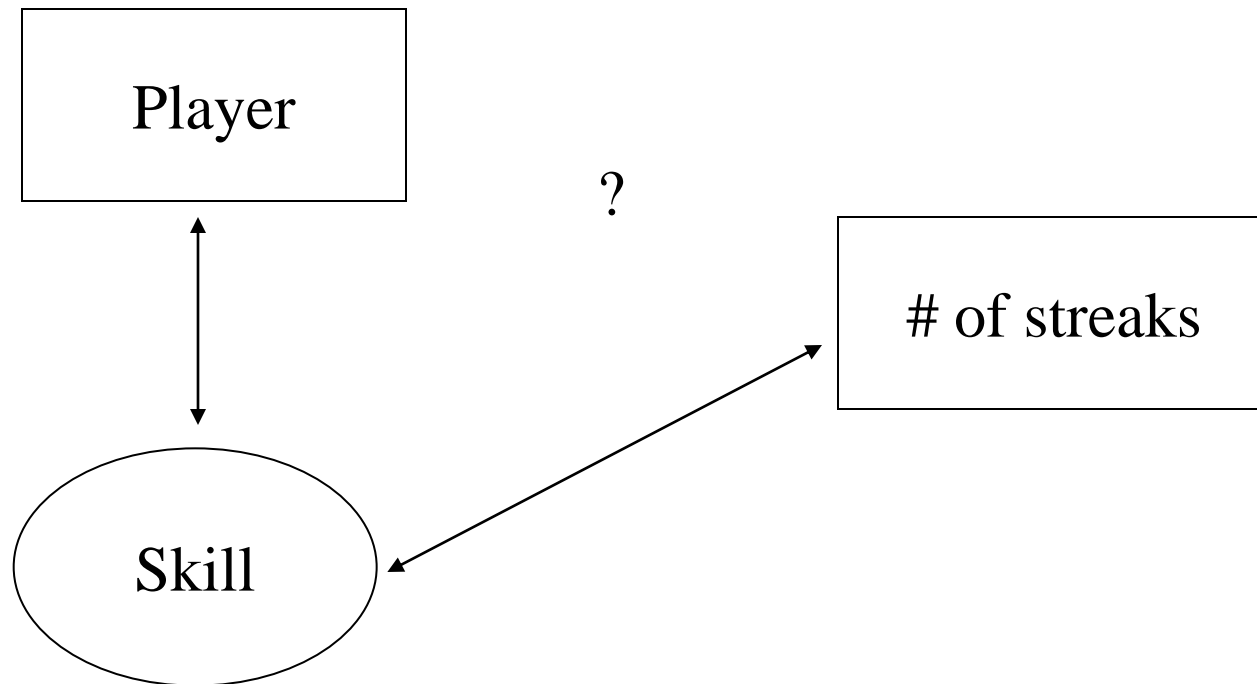
# Simpson's Paradox *Cont'd*

- High school exit exam



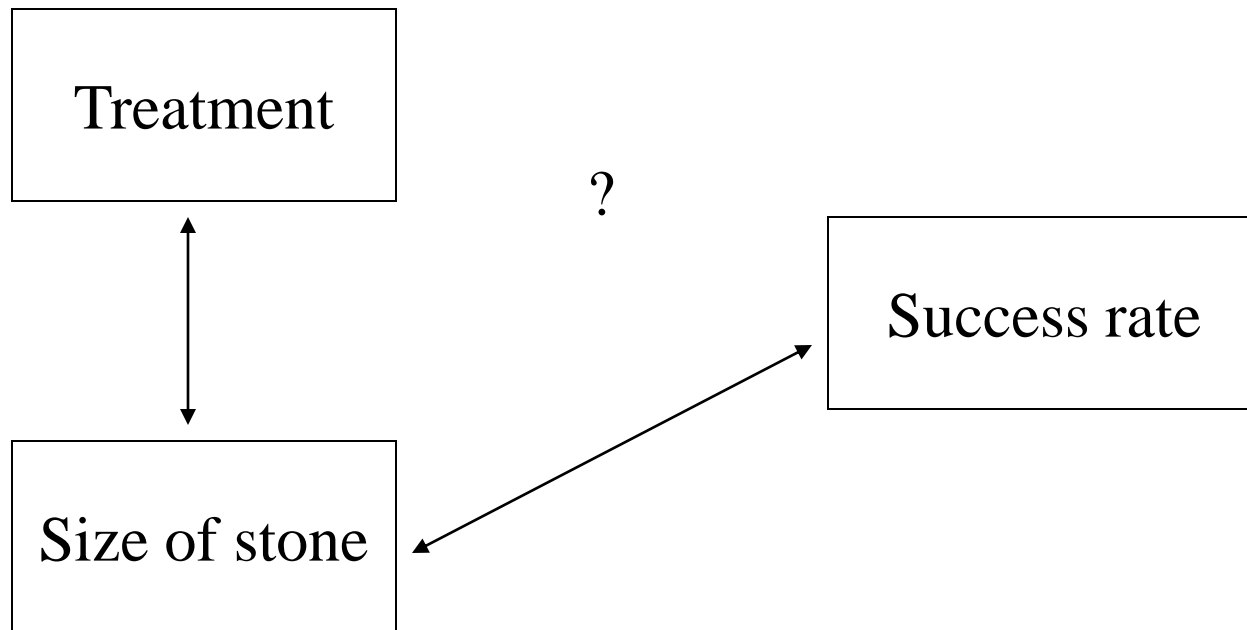
# Simpson's Paradox *Cont'd*

- Hot-hand in basketball



# Simpson's Paradox *Cont'd*

- Kidney stones



# Simpson's Paradox *Cont'd*

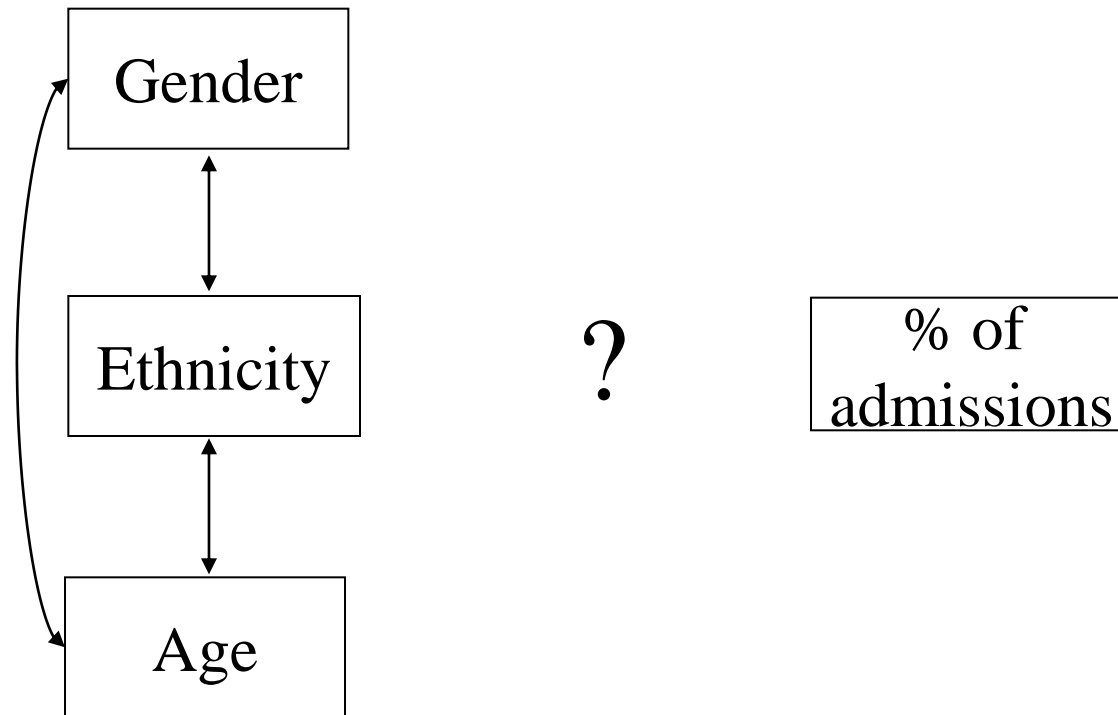
- Simpson's paradox arise easily in studies without experimental control
  - Observation studies
  - Surveys
  - Case studies
- Studies on fairness of selection typically belong to this category.

# Simpson's Paradox *Cont'd*

- A even more embarrassing version of the paradox can arise in studies of fairness with multiple groups, e.g., gender, ethnicity, and age
- Depending on the correlational structure between these groups, we may then find bias against a group in the total data set, but none, or even the opposite, in some (combination) of its subgroups

# Simpson's Paradox *Cont'd*

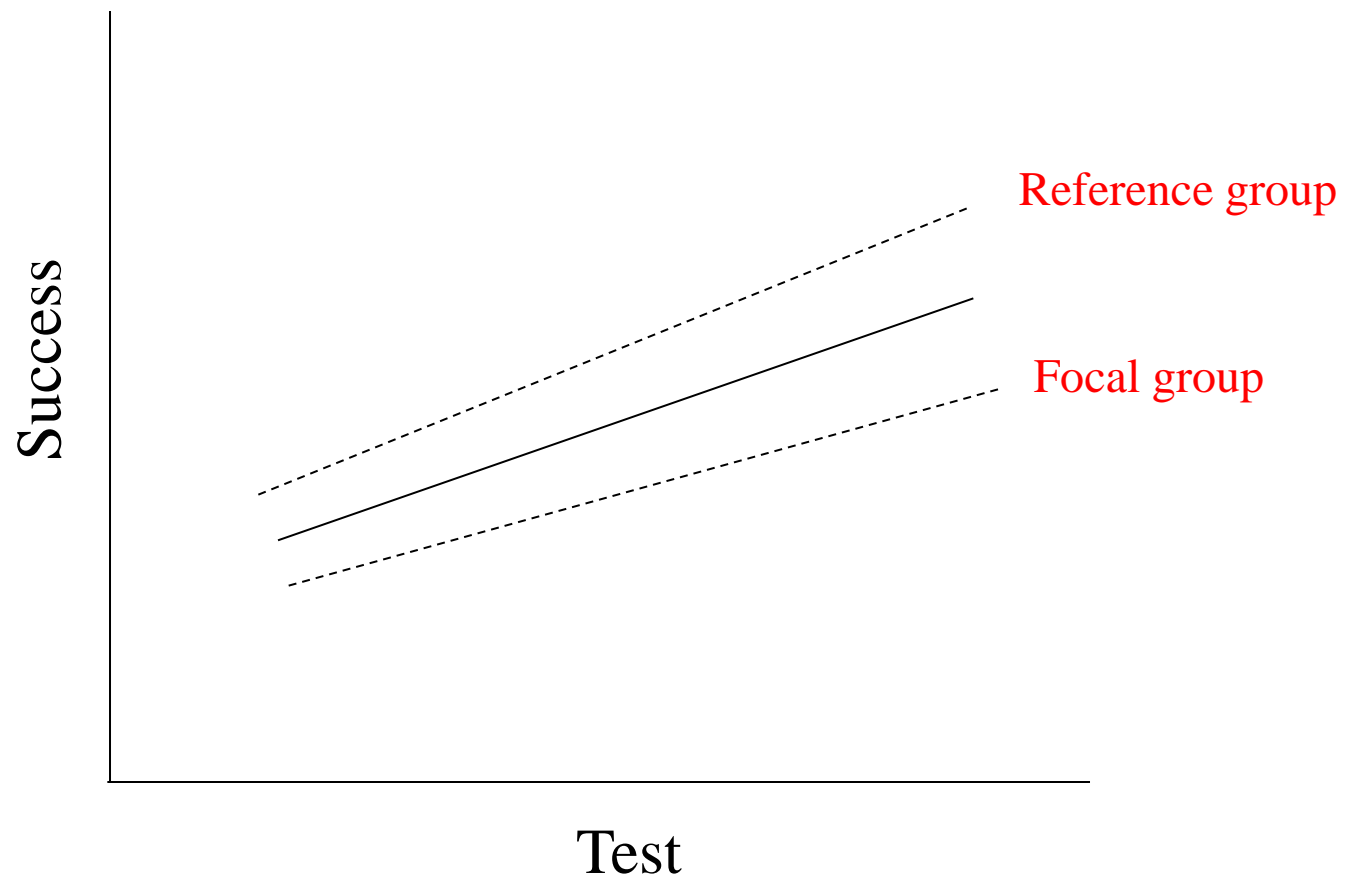
- Multiple groups



# Regression Analysis

- Evaluation of admission test as a predictor of success in the educational program
- An admission test is considered to be fair when it shows identical regression lines for the success on the test scores in the subgroups
- No distinction between bias due to
  - tests scoring (measurement bias)
  - use of inadequate predictors (prediction bias)

# Regression Analysis *Cont'd*



# Regression Analysis *Cont'd*

- Regression example from Neter & Wasserman, 1974, sect. 4.2
  - Residual plots for regression of productivity on the age of workers using machines produced by two different companies (A and B) ◻
  - Are the age measures biased? Or should we adopt another explanation?

# Regression Analysis *Cont'd*

- The typical reaction of the statistician is not to accuse the age measure of bias but look for important *missing variables* in the regression equation
- If the missing variable (here: level of experience or training) is entered in the equation, the residual plots for machine A and B become identical

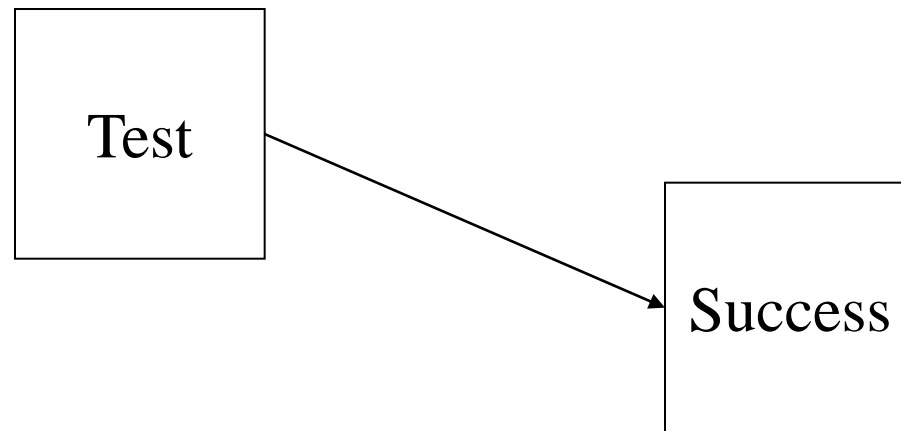
# Regression Analysis *Cont'd*

- Principle of complete modeling: If for a population of candidates all relevant predictors are in the regression equation, then the lines for any two subpopulations are identical.  
Hence,
  - if the model is complete, no “prediction bias”
  - if there is “prediction bias”, the model is not complete

# Regression Analysis *Cont'd*

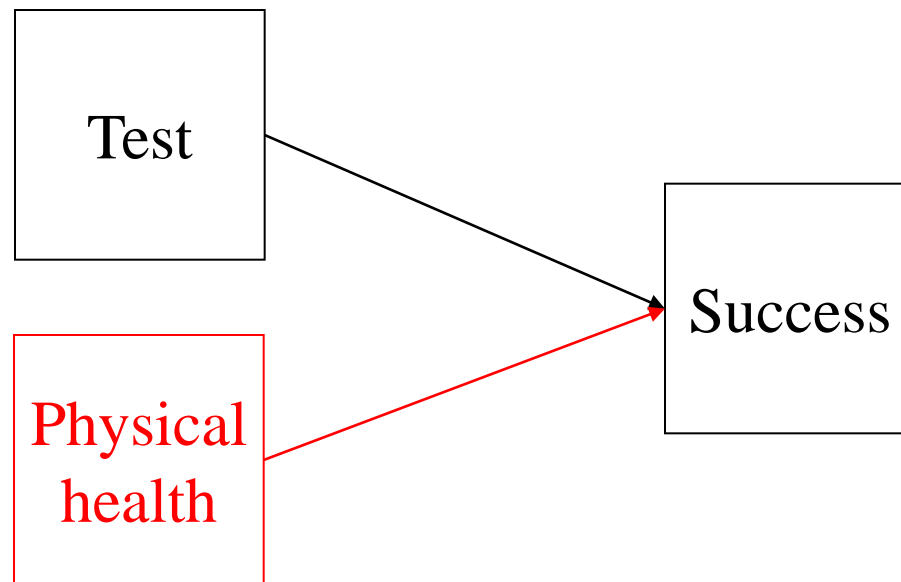
- Examples of likely missing predictors in selection to higher education: other abilities, physical health, personal income, age, gender, psychological stability, religious background, etc.
- Ethical dilemma: fairness of selection vs. acceptance of undesirable predictors

# Complete Prediction Model



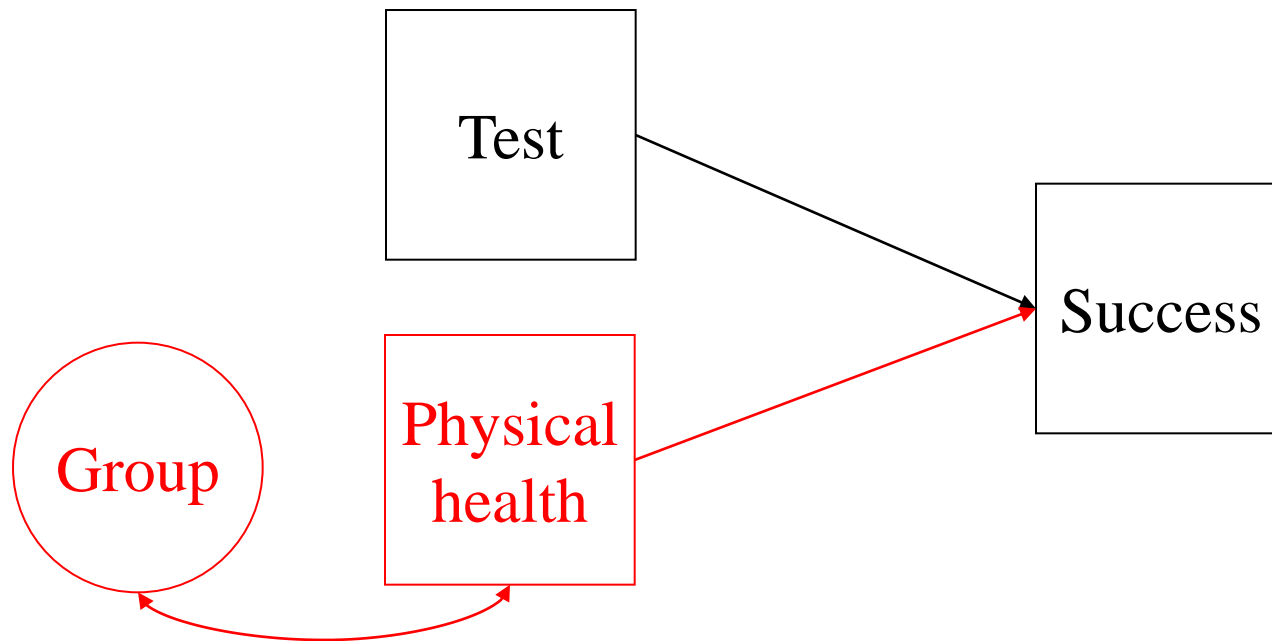
Except for random error, test scores predict all differences in success between candidates

# Incomplete Prediction Model



Individual prediction bias: success of candidates with better health is underestimated

# Incomplete Prediction Model with Groups Variable



If a group variable correlates with health, success of candidates in underestimated in one group and overestimated in the other



# Solutions?

- Controlled experiments
  - Role players as applicants
  - Manipulation of personal files
- Transition from selection testing to mastery testing
  - Two different educational systems ◻
  - Stimulation of critical program choices, etc.



# Two Different Educational Systems

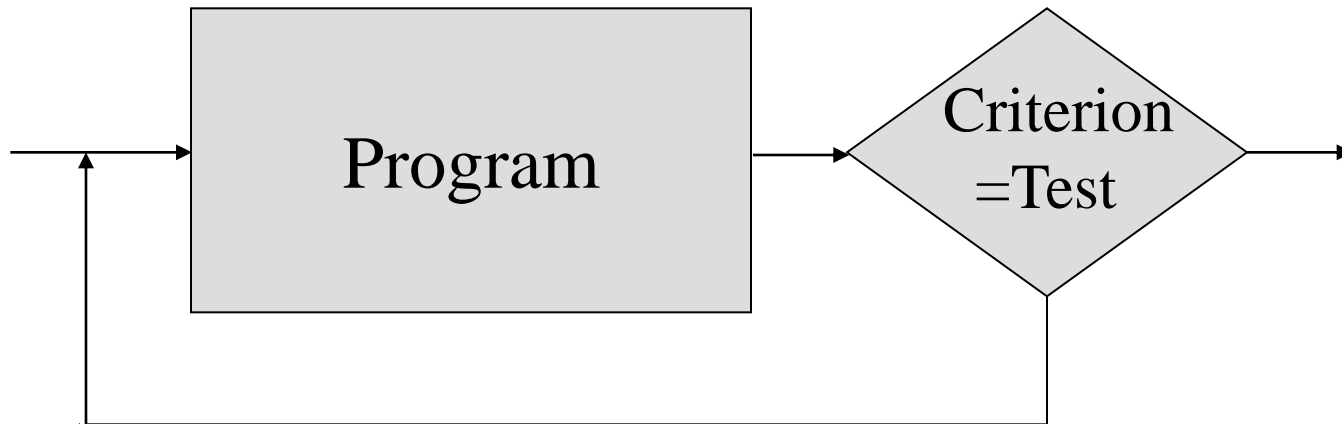
- Output control
  - National standards
  - National exit exams
  - High-school diplomas give admission rights to higher education
  - Diploma includes certification
- Input control
  - Local standards
  - National admission tests
  - High-school diplomas without admission rights to higher education
  - Separate certification

# Two Different Educational Systems *Cont'd*

- Mastery testing vs. selection testing ◻
- Achievement testing vs. aptitude testing
- Content validity vs. predictive validity
- Weak vs. fierce debates on item and test bias



# Mastery Decision



# Selection Decision

